

# What is Torsion in Shafts?

## Worksheet

Torsion is the twisting of a shaft under torque. Shear stress and angle of twist are calculated using  $\tau = Tr/J$  and  $\theta = TL/GJ$ .

$$\tau = Tr/J \text{ and } \theta = TL/GJ$$

## Questions

1. Shear stress is proportional to

- A) torque only
- B) radius only
- C) torque radius
- D) torque / (radius J)

2. Polar moment J for solid circular shaft?

- A)  $r^4$
- B)  $r^3$
- C)  $r^4/32$
- D)  $2r$

3. Larger shear modulus G means

- A) more twist
- B) less twist
- C) same twist
- D) no effect

4. Unit of polar moment J?

- A) m
- B)  $m^4$
- C)  $m^3$
- D)  $m^2$

5. Solid shaft radius 0.05 m, polar moment  $J = 4.910 \text{ m}^4$ , torque 500 Nm. Max shear stress?

6. Steel shaft 2 m long ( $G = 80 \text{ GPa}$ ,  $J = 110 \text{ m}^4$ ), torque 300 Nm. Angle of twist?

7. Hollow shaft inner 0.04 m, outer 0.06 m, torque 800 Nm.  $J = (r_o^4 - r_i^4)/32$ .  $\theta_{\text{max}}$ ?

8. Define: What is torsion in a shaft?

9. Define: Shear stress formula?

10. Define: Angle of twist formula?

## Answer Key

1. C) torque radius - =  $Tr/J$  - increases with both torque and distance from center.
2. C)  $r/32 - J = r/32$  for solid shaft, or  $d/32$  using diameter.
3. B) less twist - =  $TL/(GJ)$  - larger G decreases angle of twist.
4. C) m - Polar moment has units  $m^4$  (similar to second moment in bending).
5.  $\tau_{max} = Tr/J$   $\tau_{max} = (500 \cdot 0.05)/(4.910)$   $\tau_{max} = 25/(4.910) = 510,204 \text{ Pa} = 51 \text{ MPa}$
6.  $\theta = TL/(GJ) = (300 \cdot 2)/(8010 \cdot 110) = 600/(810) = 7.510 \text{ rad} = 0.0043$
7.  $J = (0.060 \cdot 0.04)^3/32 = 1.1610 \text{ m}^4$   $\tau_{max} = (800 \cdot 0.06)/(1.1610) = 4.14 \text{ MPa}$
8. Twisting deformation caused by torque, causing shear stress and angle of twist.
9.  $\tau = Tr/J$ , where T is torque, r is radius, J is polar moment of inertia.
10.  $\theta = TL/(GJ)$ , where L is length and G is shear modulus.

### Bounlu

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